

Bolted Joint Design

Introduction

A most important factor is machine design, and structural design is the rigid fastening together of different components. This should include the following considerations..

- Assembly
- Accuracy of positioning
- Ability to Hold components rigidly together against all forces
- Requirement to separate components
- Retention of fastening over time

There are many methods of fastening items together including

- Bolting
- Riveting
- Pins
- Keys
- Welding/Soldering/Brazing
- Bonding
- Velcro
- Magnetism

These notes relate primarily to the bolted joint. The bolted joint is a very popular method of fastening components together. The prime reason for selecting bolts as opposed to welding, or rivets is that the connection can be easily released allowing disassembly, maintenance and/or inspection..

The bolts /screws are generally used in groups to fasten plates together. A bolt is a screwed fastener with a head, designed to be used with a nut. A screw is a fastener designed to be used with a formed female thread in one of the components being attached.

These notes generally relate to bolts and nuts and hex headed screws..

Bolt loading

A bolt can be loaded in one of three ways

- Tension
- Shear
- Combined Shear and Tension

Note: Conditions where bending loads are imposed on the bolt e.g. non-parallel bolting surfaces, should be avoided.

A bolt is primarily designed to withstand tensile loading while clamping components together. Ideally the bolt should only be loaded in tension. Any forces tending to slide the clamped components laterally should be withstood by separate means..

Holes for bolts are generally clearance holes and the best design of bolt is one with a reduced shank diameter (waisted shanks). Joints in shear depending on the bolts to withstand the shear load are not really rigid. Significant relative sideways movement must take place before the bolt shank can take any shear load (hole clearance). It is also likely that in the case of components attached by a number of bolts that one bolt would be loaded first and this bolt would have to yield before the other bolts take their share of the shear load....

Bolts taking significant tensile and shear load need to be engineered to withstand the combined stress..

In structural engineering the codes identify the use of High Strength Friction Grip Bolts (Ref BS 4604 Pts 1-2:1970). The bolts are tightened to a specified minimum shank tension so that transverse loads are transferred across the joint by friction between the plates rather than by shear across the bolt shank.

In mechanical engineering / machine engineering, items are often accurately located using dowels /locating pins. When installed these dowels /locating pins should be engineered to withstand any traverse loads. A recent innovation is to provide dowel bushings. These

are used in conjunction with bolts which pass through the inside of the bushing after it has been installed. Separate holes for locating pins are eliminated. The hardened bushings absorb shear loads, isolating the bolts from these forces.

If the choice is made that bolts/screws are to take shear load the joint should be arranged that the threaded portion of the bolt/screw shank is not taking the shear.

The notes on this page relate to the mechanical engineering industry.. In the aerospace industry joints are often designed to specifically load the bolts in shear. The screws and bolts used are high specification close tolerance items and the holes are also machined to close tolerances. The bolted lap joints are generally used for critical assemblies and joints designed with bolts loaded in tension are avoided.????

Strength of Bolts in Shear

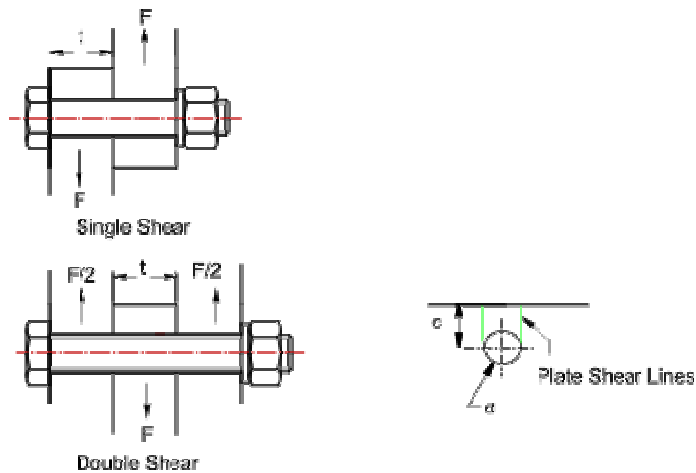
Important Note:

The calculations below are based on the unrealistic assumption that there is no friction forces between the plates which are clamped by the bolts. The calculations are therefore conservative (safe)..

Strength of Bolts withstanding direct shear loading

For bolts joints loaded in shear - three stress areas result-

- The bolts are loaded in shear. Depending on the joint design the bolt can be in single or double shear...
- The bolt interface with the hole is compressively loaded. (Crushing)
- If the hole is near to the edge of the plate the plate is subject to shear loading



Single Shear..

$$\begin{aligned} \text{Shear Stress} &= 4 \cdot F / \pi \cdot d^2 \\ \text{Compressive Stress} &= F / (d \cdot t) \\ \text{Plate Shear Stress} &= F / (2 \cdot c \cdot t) \end{aligned}$$

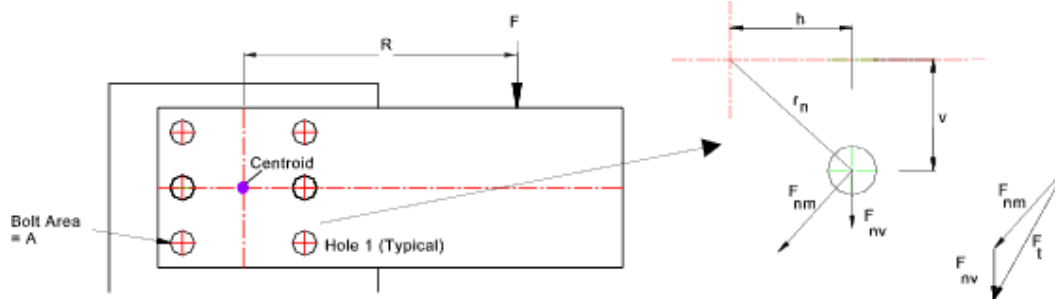
Double Shear ..

$$\begin{aligned} \text{Shear Stress} &= 2 \cdot F / \pi \cdot d^2 \\ \text{Compressive Stress} &= F / (d \cdot t) \\ \text{Plate Shear Stress} &= F / (2 \cdot c \cdot t) \end{aligned}$$

The stresses are adjusted based on the number of bolts / screws used for the joint..

Strength of bolts withstanding torsion generated shear loading

Consider a bracket taking an offset load F (N) at a radius R (m). The bracket is secure using a number of bolts each with a Area A(m²). The bolts are located around a centroid position each with a radius from the centroid of r_n(m) and a horizontal/vertical position relative to the centroid of h_n / v_n (m) . (bolt is designated by the subscript "n".)



Location of Centroid...

The location of the centroid of the bolts can often be determined by inspection as in figure above. If the bolts are not arranged around a convenient centre then the centroid is determined by ..
 x position = sum of the moments of area of all the holes about a fixed horizontal position divided by the total hole area
 y position = sum of the moments of area of all the holes about a fixed vertical position divided by the total hole area

The offset load is equivalent to a vertical force (F) + moment (F . R) at the centroid of the bolts...

Each bolt withstands a vertical shear force $F_{nv} = F / \text{No of Bolts}$.

Each bolt also withstands a shear load $F_{nm} = F \cdot R \cdot r_n / (r_1^2 + r_2^2 \dots r_n^2)$

The total horizontal force on each bolt $F_{th} = F_{nm} \cdot v_n / \text{Sqrt}(h_n^2 + v_n^2)$

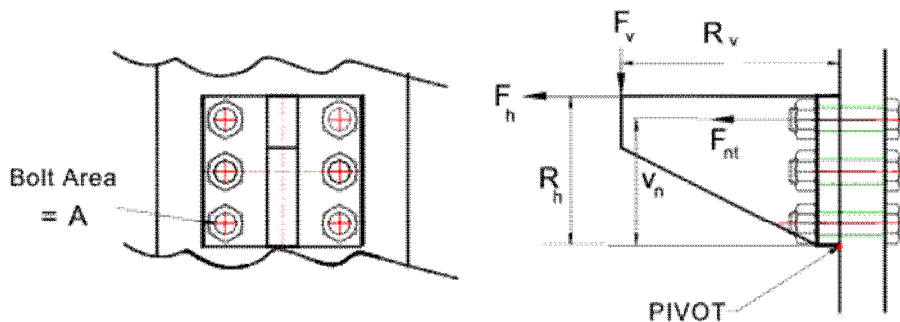
The total vertical force on each bolt $F_v = F_{nv} + F_{nm} \cdot h_n / \text{Sqrt}(h_n^2 + v_n^2)$

The total shear load on each bolt $F_t = \text{Sqrt}(F_{th}^2 + F_v^2)$

The resulting bolt shear stress $\tau = F_t / A$

The shear stress in each bolt is calculated to ensure the design is safe..

Strength of bolt joints withstanding bending forces



Each Bolt withstands a shear Force $F_s = F_v / (\text{Number of bolts})$

The resulting shear bolt stress $\tau_n = F_s / A$

Note: Each bolt is assumed to withstand the same shear force.

If there are x bolts(numbered n = 1 to x). Then the tensile force withstood by each bolt is designated F_{nt} i.e $F_{1t}, F_{2t}, F_{3t} \dots F_{xt}$

A selected bolt (n) withstands a tensile force of $F_{nt} = (F_v \cdot R_v + F_h \cdot R_h) \cdot V_n / (V_1^2 + V_2^2 \dots V_x^2)$

The resulting tensile bolt stress $\sigma_n = F_{nt} / A$

Maximum principals stresses in the bolt resulting from combined loading

The notes on this page Assuming all stresses developed only as a result of bracket loading i.e zero preload and zero residual bolt torque...

Maximum principal tensile stress in the bolt

$$\sigma_1 = \frac{\sigma_n}{2} + \frac{1}{2} \sqrt{\sigma_n^2 + 4 \tau_n^2}$$

Maximum principal compressive stress in the bolt

$$\sigma_3 = \frac{\sigma_n}{2} - \frac{1}{2} \sqrt{\sigma_n^2 + 4 \tau_n^2}$$

Maximum shear stress in the bolt

$$\tau = \frac{1}{2} \sqrt{\sigma_n^2 + 4 \tau_n^2}$$

Failure criteria: Refer to page [Failure Modes](#)

The notes on this page In order to estimate the design factors of safety it is necessary to consider the failure modes. The preferred failure criteria for ductile metals is the "Shear Strain Energy Theory" (Von Mises-Hencky theory). For a stress regime associated with a bolt i.e pure tensile stress σ_x combined with shear stress τ_{xy} . The Factor of safety relative to the material tensile strength S_y ..is calculated as follows

$$\text{Factor of Safety} = S_y / (\sigma_x^2 + 3 \tau_{xy}^2)^{1/2}$$

Preloaded Bolts : Refer to page [Preloading](#)

These stresses do not include for the stresses developed in preloading the bolts. The residual shear stress from bolt tightening should also considered (added). The actual tensile preload force should be considered following the principles identified on the pages addressing this topic

Breaking Load in Single Shear – kN

Standard	AS1111 P.C. 4.6		AS1110 P.C. 8.8			AS1110 P.C. 10.9		
	AS2451 Grade 2		AS2465 Grade 5			AS2465 Grade 8		
Diameter	Shank	Thread	Shank	Thread		Shank	Thread	
				Coarse	Fine		Coarse	Fine
M6	7	4	14	9		18	12	
1/4"	9	5	16	9	11	20	11	14
M8	13	8	25	16		32	21	
5/16"	13	8	25	15	17	32	19	22
3/8"	19	12	37	23	27	46	28	34
M10	20	13	39	26		51	34	
7/16"	26	16	50	31	36	63	39	45
M12	28	19	57	38		74	50	
1/2"	34	21	65	42	50	82	52	62
M16	50	36	101	72		131	94	
5/8"	53	35	102	67	80	128	84	100
3/4"	77	53	147	101	117	184	126	146
M20	79	56	163	117		204	146	
M22	94	67	196	140		245	175	
7/8"	105	73	201	140	160	251	175	200
M24	113	81	235	168		294	211	
1"	137	97	262	184	208	327	230	260
M27	142	102	295	212		369	266	
1.1/8"	173	121	332	202	237	414	289	338
M30	177	130	368	270		459	337	
1.1/4"	214	150	367	273	310	524	390	443
M36	254	190	529	395		662	493	
1.1/2"	308	226	589	377	444	736	539	637